Backward Difference Approximation of the First Derivative

We know

$$f'(x) = \lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

For a finite Δx ,

$$f'(x) \approx \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

If Δx is chosen as a negative number,

$$f'(x) \approx \frac{f(x + \Delta x) - f(x)}{\Delta x}$$
$$= \frac{f(x) - f(x - \Delta x)}{\Delta x}$$

This is a backward difference approximation as you are taking a point backward from x. To find the value of f'(x) at $x = x_i$, we may choose another point Δx behind as $x = x_{i-1}$. This gives

$$f'(x_{i}) \approx \frac{f(x_{i}) - f(x_{i-1})}{\Delta x} \\ = \frac{f(x_{i}) - f(x_{i-1})}{x_{i} - x_{i-1}}$$

where

$$\Delta x = x_i - x_{i-1}$$



Figure 2 Graphical representation of backward difference approximation of first derivative.